

# Task Scheduling in Distributed Systems by Work Stealing and Mugging — A Simulation Study

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We model and simulate the execution of parallel jobs represented by directed acyclic graphs on a system of networked distributed heterogeneous computers. We tested two online schedulers, the Enhanced Cilk Scheduler (*ECS*) and the Central Manager (*CM*). *ECS* is a decentralized scheduler, which implements work stealing and processor mugging techniques. *CM* is a centralized greedy scheduler. Our simulation results show that *ECS* is a well behaved scheduler particularly suited for scheduling task execution in dynamically changing systems because it is robust, requires little communication, and almost matches the performance of the *CM* scheduler.

*Keywords:* distributed systems, parallel computing, scheduling, simulation.

## 1. Introduction

One of the basic problems in parallel computing is how to execute a parallel program on a collection of *heterogeneous* processors, that is, processors of different and possibly changing speeds. In this paper we simulate scheduling algorithms that are designed to run efficiently in heterogeneous parallel computing environments.

We model and simulate the execution of parallel jobs represented by directed acyclic graphs (DAG). Each job is a multi-threaded parallel program. A thread is a chain of tasks ordered by their execution dependencies. Dependencies of the tasks/threads in a job are represented by a DAG. The nodes in a DAG correspond to tasks and directed edges represent precedence relationship among tasks.

We study two online schedulers — the *Enhanced Cilk Scheduler (ECS)* and the *Central Manager (CM)*. *Work stealing* [6, 7] and *processor mugging* techniques are central to *ECS* making a low-overhead, non-centralized, and fault-tolerant scheduler with provable [5] performance guarantees. A centralized omnipotent greedy scheduler, we call *Central Manager*, is the benchmark we use to assess the *ECS* performance.

Applications of decentralized adaptive online scheduling algorithms include web-based computing, utilizing idle processors within organizations, scientific computing, military applications, etc. Related work is found in the area of asynchronous parallel computing [1, 3, 4, 2, 9] as well as in scheduling theory [8].

In our simulation, *ECS* runs efficiently even when processors have different and dynamically changing speeds. *ECS* is robust, it is scalable because it is distributed, and it is a fault tolerant scheduler. The quality of schedules exhibited by *ECS* is almost as good as that of centrally managed ones.

## 2. Experimental Study

We study a scheduling problem in a networked system of heterogeneous processors. Each processor is described by its set of attributes: maximum speed, current speed, and steal-mug interval (the time between attempts by the processor to steal/mug work from other processors). Our model also allows for changes in the speeds of processors.

Our study compares two types of schedulers on a network of heterogeneous processors, that is, processors of different (fixed or changing) speeds. The *Enhanced Cilk Scheduler (ECS)* (see Fig. 1), is based on a non-centrally managed randomized model that employs steals and muggings. The centrally managed scheduler, or *Central Manager (CM)* uses a simple greedy heuristic to assign subtasks to processors, but relies on tightly coupled centralized control.

#### ENHANCED CILK SCHEDULER

1. Processor  $i$  chooses a victim processor  $j$  uniformly at random.
2. If the victim  $j$ 's double ended queue (deque) is not empty, it steals the thread  $T$  from the *top* of the deque.
3. If the victim  $j$ 's deque is empty, but the victim is working on a thread  $T$  and it is slower than processor  $i$ , then  $i$  mugs  $j$ , that is,  $i$  interrupts  $j$  and takes the thread  $T$ .
4. If processor  $i$  has located a thread  $T$ ,  $i$  works on  $T$  until one of four situations:
  - a) Thread  $T$  spawns  $k$  new threads. In this case, the processor puts  $T$  and, one by one,  $k - 1$  new threads in order of appearance, on the *bottom* of the ready deque and starts work on the *last* spawned new thread.
  - b) The thread  $T$  returns or terminates. If the deque is not empty, the processor begins working on the *bottom* thread. If the deque is empty, the processor attempts to work steal.
  - c) The thread reaches a synchronization point. In this case, the processor attempts to work steal. (Note that the deque is empty.)
  - d) Processor  $i$  is mugged and the thread  $T$  is migrated to another processor. In this case, processor  $i$  attempts to work steal.
5. Otherwise, there is a failed steal attempt; processor  $i$  tries to steal again.

Fig. 1. The Enhanced Cilk Scheduler.

The *ECS* attempts to complete tasks in the network as quickly as possible by using *work stealing* or *processor mugging*. Work stealing happens when an idle processor takes a ready task from a busy processor's queue and begins executing it. An idle processor  $P_f$  performs processor mugging when it encounters a slower processor  $P_s$  executing a task  $T$  and the queue of  $P_s$  is empty. In that case,  $P_f$  takes over the execution of task  $T$  and processor  $P_s$  becomes idle and starts looking for work. In *ECS*, the "victim" processor is chosen at random, uniformly among all other processors in the system. Attempts to steal/mug occur at regular intervals

(specified by the steal/mug interval), whose lengths are inversely proportional to the speed of the processor exercising the stealing/mugging.

The *CM* scheduler applies a greedy strategy. It keeps a FIFO queue of the ready-to-process threads and assigns a thread to the currently fastest idle processor. When some processor  $P_i$  becomes idle and the queue is empty, the *CM* scheduler possibly assigns a task to it: if the slowest active processor  $P_s$  is slower than  $P_i$ , then the *CM* reassigns the work on the active processor to  $P_i$ , effectively "mugging"  $P_s$  by central authority.

Both the *ECS* and *CM* use *preemption*: each task can be preempted, or interrupted and continued on some faster processor. (This means that we are assuming checkpointing or other support in order to enable essentially continuous preemption and restart.)

In both models, the experimental results reported here have the migration cost set to zero (i.e., there is no calculated delay in migrating a task, whether by stealing, mugging, or assignment by the central manager). Instead, we calculate these communication costs separately because different platforms have different communication costs.

Our simulation program is written in Simscript II.5. Processor features, system utilization, network topology, and characteristics of jobs (DAGs) are part of the input. Experiments were conducted on a Sun Ultra 30 with 512 MB memory, running Solaris 2.6. Comparison of *CM* vs. *ECS* in several contexts is performed with promising results.

## 2.1. Experiment 1

In this experiment, the input DAG consists of a "fan out" (from a single node to 50 nodes) followed by a "fan in" (back to a single node). All tasks are uniform in this case: each of the nodes in the middle of the DAG correspond to tasks requiring 50000 work units. This experiment is meant to model the case in which the job is readily parallelized into equal-sized subtasks, which are readily combined into the final output. (Note that in the traditional Cilk implementation [7], each thread can fork into only two threads at the time.) The system is comprised of

8 networked processors. The processors have various speeds: one works at 100 work units per unit time (*ms*), one at 200, one at 300, two at 400, two at 800, and one at 1600 work units per unit time. Communication cost is zero along edges of the network, since we count migrations separately.

Time interval  $I_0$  denotes initial steal/mug interval, that is approximately proportional to the reciprocal of the processor speed. Specifically, the interval is 1 *ms* for the processor of speed 100, 0.7 for the processor of speed 200, 0.5 for the processor of speed 300, 0.3 for the processors of speed 400, 0.1 for the processors of speed 800, and 0.05 for the processor of speed 1600. In (Tables 1–2), we show the data for values of steal/mug interval ranging from  $I_0/64$  up to  $512I_0$ . This broad range allows us to see how the speed approaches an asymptote as the steal/mug interval approaches zero and how the performance deteriorates as this interval increases. For each steal/mug interval, we ran the simulation 500 times, for every run the processor initiating DAG execution is selected uniformly at random. We tabulated minimum, average, maximum, standard deviation for the completion time and average numbers of successful steals and muggings over the 500 runs.

Two main lower bounds on the time required to complete a DAG in this setting are total work of

Steal/Mug	Min	Avg	Max	$\sigma$	$N_S$	$N_M$
$I_0/64$	613.4	621.4	627.4	3.05	33.9	48.6
$I_0/32$	612.2	621.5	628.1	2.90	33.8	48.4
$I_0/16$	612.7	621.8	628.3	2.95	33.9	48.5
$I_0/8$	613.9	621.8	628.3	3.07	33.8	48.2
$I_0/4$	615.0	622.6	629.3	3.01	33.8	48.8
$I_0/2$	615.2	624.2	630.5	3.06	33.7	48.2
$I_0$	617.0	626.7	634.6	3.20	33.6	47.9
$2I_0$	618.3	631.8	642.4	3.81	33.2	45.9
$4I_0$	629.1	642.8	656.8	5.32	32.9	43.9
$8I_0$	641.5	663.7	699.8	9.07	32.2	40.3
$16I_0$	663.1	701.0	746.9	15.12	31.0	34.0
$32I_0$	692.2	766.1	868.2	25.19	29.0	26.9
$64I_0$	738.9	871.7	1031.0	44.21	26.2	19.8
$128I_0$	870.2	1043.1	1392.7	94.15	23.1	13.9
$256I_0$	1019.2	1314.5	2156.7	203.05	20.2	9.8
$512I_0$	1150.6	1707.1	3302.1	445.30	16.5	6.2

Table 1. Simulation data for Experiment 1, using Enhanced Cilk Scheduler (ECS).

DAG divided by sum of processor speeds, and critical path divided by the speed of the fastest processor. However for this special case there is a better lower bound, obtained as follows. First, the sum of the speeds of the 8 processors is 4600 work units per unit time. The best we can hope to do is to process the first task (node) with the fastest processor in time  $50\,000/1600$ , then the 50 middle tasks in time  $50 \cdot 50\,000/4600$ , then the final task (after fan-in) with the fastest processor in time  $50\,000/1600$ . This gives a lower bound of 605.98 time units to complete the DAG. In comparing with this lower bound, we see that the ECS method, using the most frequent steal/mug attempts ( $I_0/64$ ), performs within 2.5% of lower bound, on average, with the maximum completion time among the 500 runs only 3.5% worse than lower bound for this experiment.

Steal/Mug	Min	Avg	Max	$\sigma$	$N_S$	$N_M$
N/A	623.1	623.1	623.1	.00	41.1	6.6

Table 2. Simulation data for Experiment 1, using the central manager scheduler (CM).

The average performance of ECS degrades as the steal/mug intervals increase asymptotically reaching times when there are no steals and muggings. Still, for steal/mug intervals of  $16I_0$ , on average ECS is lagging 15% behind the lower bound for the configuration, executing 31 steals and 34 muggings on average, compared to average of 34 steals and 49 muggings when attempts are most frequent ( $I_0/64$ ).

The average number of steals decreases with the steal/mug interval. Muggings decrease more steeply. This behavior is expected, since once the first task is over, 50 tasks are released and put in the queue of the processor that just completed the first task. A smaller number of attempts results in a smaller number of successful steals or muggings.

The completion times and their volatility for the given configuration are increasing with the decreasing rate of steal/mug attempts. Because of infrequent steal/mug attempts and random choice of the “victim”, faster processors can stay idle longer while slower processors are busy, thus increasing completion time.

## 2.2. Experiment 2

In this experiment, the input task DAG (Fig. 2) consists of a task of size 16 000, which fans out to 50 parallel tasks, each of size 50 000, then fans in to a task of size 16 000, then fans out to 6 parallel tasks of size 500 000 each, then finally fans in to a task of size 16 000. This experiment is meant to model the case in which the job is initially parallelized into many equal-sized subtasks, which are then combined and a small number of follow-up tasks are run in parallel. This DAG models some practical image-object recognition applications, as the large fan-out is done in the raw image processing, while the longer, narrower part of the DAG models the more time-consuming, less number-crunching tasks of feature matching and object recognition. This experiment uses a network of 12 processors. The processors have various speeds: one works at 100 work units per unit time ( $ms$ ), one at 200, one at 300, three at 400, three at 800, and three at 1600 work units per unit time. For each processor, the product of speed and time interval  $I_0$  is 80 work units. Each batch of 500 runs increases steal-mug interval 20% in respect to the previous batch. Each run starts on a randomly selected processor. Task migrations are counted separately.

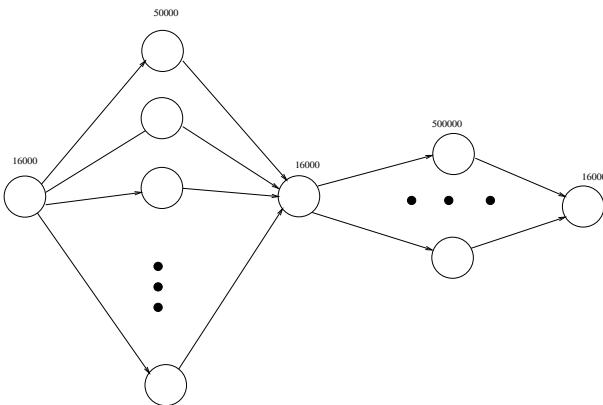


Fig. 2. The DAG for Experiment 2.

We can compute readily a lower bound on the processing time of the DAG, by keeping the maximum possible number of fastest processors busy all the time in each phase (e.g., in the second parallel phase of the DAG we have 6 tasks so only 6 fastest processors can be employed simultaneously). The resulting bound is 724.44 time units.

Steal/Mug	Min	Avg	Max	$\sigma$	$N_S$	$N_M$
$I_0$	788.70	796.38	804.01	2.75	46.9	74.2
$(1.2)I_0$	789.36	797.50	805.29	2.86	46.9	73.8
$(1.2)^2I_0$	790.54	798.64	808.10	3.04	46.8	72.9
$(1.2)^3I_0$	792.20	800.17	808.72	2.92	46.7	72.3
$(1.2)^4I_0$	792.33	801.72	809.13	3.10	46.5	71.1
$(1.2)^5I_0$	792.34	803.61	820.46	3.48	46.4	70.0
$(1.2)^6I_0$	796.39	806.52	820.25	3.67	46.3	69.7
$(1.2)^7I_0$	798.90	809.75	821.28	4.26	46.1	68.0
$(1.2)^8I_0$	800.96	812.75	825.12	4.39	46.1	66.7
$(1.2)^9I_0$	804.80	817.58	840.77	5.21	46.0	65.4

Table 3. Simulation data for Experiment 2, using the enhanced Cilk scheduler (ECS).

Steal/Mug	Min	Avg	Max	$\sigma$	$N_S$	$N_M$
N/A	795.62	795.62	795.62	0.	59.3	10.6

Table 4. Simulation data for Experiment 2, using the central manager scheduler (CM).

Refer to (Tables 3–4). On average, *ECS* run with the most frequent steal/mug attempts is 10% above the lower bound. This lag is mostly due to “persistence” of fast processors; i.e., once they grab a task, it will be processed completely. For experiment, 2 processors, with the first being twice as fast as the second one, work on 2 equally long tasks. It would be efficient to swap tasks at halftime of the optimal run. That way, both would be active from the beginning to the end. Instead, the faster processor finishes his task first and then takes over the other, leaving the slower processor idle.

## 2.3. Experiment 3

This experiment runs simulations of the *ECS* system with *changing* speeds of processors. In the following set of simulations, we tested *ECS* method robustness to processors’ speed change, as may be expected to occur in real systems. Processors change speed in a stepwise manner (an alternating renewal process); i.e. they start working full speed and, after some randomly generated time with exponential distribution,

speed drops down to a level randomly chosen from a uniform distribution between two input parameters: minimum and maximum percentage of full speed. After the exponential random time of a processor working at full speed, the speed changing pattern is repeated. We executed five simulations and compared average completion times with the system in which processors work full speed all the time. Each simulation is executed for 100 DAGs of “graphic” and “fan-out-fan-in” type. This experiment employs a network of 12 processors. The processors have various speeds: one works at 100 work units per unit time (*ms*), one at 200, one at 300, two at 400, four at 800, and three at 1600 work units per unit time. For each processor, the product of speed and steal/mug interval is 80 work units. Communication cost for task migration is zero along the edges of the network. For each simulation run, the duration of both full speed periods and reduced speed periods are randomly chosen from an exponential distribution with the mean of 50 time units.

DAG	100	80-100	60-80	50-70	40-60	10-50
Graphic	785	825	917	939	1018	1097
Fan-out.	346	361	397	407	441	493

Table 5. Average execution times when processors exhibit speed change.

Refer to Table 5. The top row denotes speed range during the slowdown phase as the percentage of full speed. The first data column is the benchmark – when speeds do not change. In the first run, speeds are only reduced to between 80 and 100%. Consecutive simulations are reducing processor speeds to 60-80%, 50-70%, 40-60%, and finally to 10-50%. As the overall system computing power decreases, the completion times are decreasing linearly. Thus, *ECS* performance degrades gracefully with changes of processor speeds.

## 2.4. Experiment 4

In this experiment, we simulate a networked system of 100 processors. Their speeds range

from 1600 down to 100 (17 processors of speed 1600, 29 of speed 800, 25 of speed 400, 12 of speed 300, 8 of speed 200 and 9 of speed 100). Two types of DAGs, “graphic” and “fan-out-fan-in” with uniformly-sized tasks (as described in Experiments 1 and 2), arrive into a system according to a Poisson process with some mean DAG inter-arrival time. At the arrival time, the type of DAG is randomly determined, according to a discrete uniform distribution. The simulation is continuous, and statistics are collected after each consecutive 1000 DAG completions. Both systems are simulated on an identical DAG arrival timeline; thus, we can directly compare the quality of scheduling schemes. Again, we simulate *ECS* and *CM* systems behavior. In the *ECS* system, processors attempt to steal/mug at the  $I_0$  level as described in Experiment 2.

The *ECS* scheme is implemented here by two queues on each processor. A *ready queue* is maintaining tasks of a DAG in process and a *waiting queue* is keeping newly arriving DAGs in FIFO order. When a DAG appears on a processor, it is processed immediately if the processor is idle. If the processor is busy, the initial task of the DAG is placed in the waiting queue. When a processor is finished with a task, successor tasks from the DAG are released and placed in the ready queue and the processor continues with the tasks from the bottom of the ready queue. If the ready queue is empty, the processor takes on the task from the top of the waiting queue. If both queues are empty, the processor attempts to steal/mug. The steal/mug procedure is as follows: the victim’s ready queue is checked first and if not empty the task from the top is stolen. If the ready queue is empty, the waiting queue is checked and the task from the top, if any, is stolen. If both queues are empty, we have a mug attempt.

The mean DAG inter-arrival time is 300 time units. The system utilization<sup>1</sup> is low, slightly above 0.2 (0.2047); thus, completion times distribution is positively skewed, i.e. more than 50% of DAGs are completed in time less than average. Longer completion times are due to peaks in DAG arrivals. Again, *CM* model performs slightly better on average but it is not penalized for polling the status of each processor in the system that usually requires enormous

<sup>1</sup> The *system utilization* is defined to be the ratio of the time integral of the active processing power to the time integral of the available processing power in the system.

amount of network traffic. *ECS* steal/mug attempts are one-on-one, requiring far less polling network traffic. On the other hand, task migrations from processor to processor are almost 50% more frequent in *ECS* than they are in *CM* system. This will lead to network traffic delays of DAG completion times (we don't incur migration costs in this experiment.) The lower bound on processing time of graphic DAG is 390.58 and our statistical analysis shows that 95% of the time that kind of DAG will be processed in time less than 534.03 time units; a result is only 37% worse than the lower bound. Half of the times that type of DAG will be processed in time less than 421.85 time units, only 8% slower than lower bound.

Refer to Fig. 3. *CM* performs slightly better than *ECS* on the “fan-out-fan-in” DAG, as expected, but the lag is small. The system is

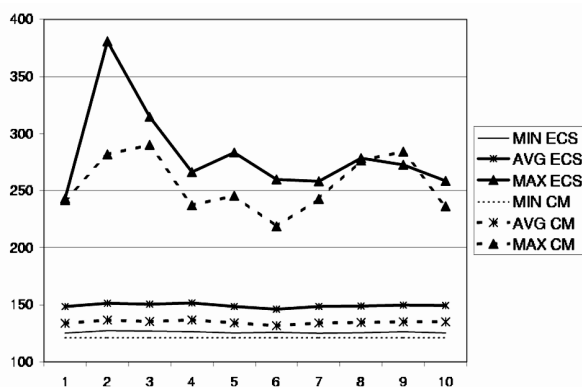


Fig. 3. The minimum, average, and maximum completion times of 10 batches of 1000 “fan-out-fan-in” DAG completions in *ECS* and *CM* scheme with system utilization of 0.2.

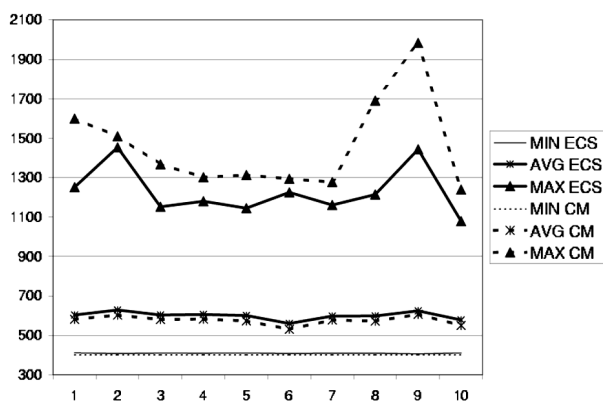


Fig. 4. The minimum, average, and maximum completion times of 10 batches of 1000 “graphic” DAG completions in *ECS* and *CM* scheme with system utilization of 0.6.

lightly loaded and DAGs are with high probability completed at most 50% beyond lower bound. The vertical axis measures time units; the horizontal axis refers to the actual runs (with marks per 1000 runs).

In Fig. 4, completion times with “graphic” DAGs batches of size 1000 are given. DAGs enter the system according to a Poisson process, with exponential inter-arrival time distribution having a mean of 100 time units. System utilization is thus increased to about 0.6 and completion times are more volatile. *CM* scheduler is still better than *ECS* on average, but it exhibits larger spreads between minimum and maximum times and maximum completion times are larger in *CM* than in *ECS*.

### 3. Conclusions

Based on our simulation results it can be stated that *ECS* is a viable well behaved scheduler in distributed heterogeneous environment. Even though *CM* was equipped with much higher degree of knowledge of overall system state, the results show that on average *ECS* is not that much slower and measured by QoS measure it performs even better. Another huge benefit of the *ECS* is its decentralized nature and adaptability versus *CM*'s centralized control. Once control unit fails or becomes unusable the whole system is rendered unusable as well (unless there is some mechanism of control component back up). On the other hand, *ECS* system participants behave according to simple local protocol and thus the system is highly scalable and resilient to failures of its elements.

Future work may include: (1) Further understanding of parallel program types; (2) Inclusion of migration costs, query costs for *CM* system, faults (within the system or coming from outside), multi-layered systems inhomogeneous processors; (3) Perform the simulation experiments with real-world parameters and compare *ECS* with Depth First (DF) and Depth First Deques (DFD); and (4) Implement the work stealing paradigm in solving graph-partitioning problems.

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